case of BDP, where $C(1) \cdots C(6)$ is $2 \cdot 30 \AA$, these values prove the minimal nature of the corresponding $\mathrm{C}-\mathrm{C}$ overlap.

All F atoms are involved in $\mathrm{H} \cdots \mathrm{F}$ distances $<2 \cdot 50$ $\AA$, an approximate value of the sum of the van der Waals radii. Two of these rather short contacts concern both H atoms at $\mathrm{C}(16)$, while no $\mathrm{H} \ldots \mathrm{F}$ distances below $2.80 \AA$ are observed for the H atoms of the other bridgehead C atom.

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# $\alpha$-L-Sorbopyranose: A Neutron Diffraction Refinement* 

By S. Nordenson $\dagger$ and Shozo Takagi $\ddagger$<br>Chemistry Department, Brookhaven National Laboratory, Upton, New York 11973, USA

and G. A. Jeffrey

Department of Crystallography, University of Pittsburgh, Pittsburgh, Pennsylvania 15260, USA
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#### Abstract

C}_{6} \mathrm{H}_{12} \mathrm{O}_{5}, M_{r}=180 \cdot 16, P 2_{1} 2_{1} 2_{1}, a=\) 6.545 (2), $b=18.062$ (7), $c=6.310$ (2) A, $D_{x}=$ $1.604, D_{m}=1.607 \mathrm{Mg} \mathrm{m}^{-3}, V=745.94 \AA^{3}$. More accurate dimensions were obtained and the disorder in the orientation of the primary alcohol group, observed in the previous X-ray study [ Kim \& Rosenstein (1967). Acta Cryst. 22, 648-656], is confirmed and better defined. The gauche/trans orientation of the primary alcohol hydroxyl group has 0.625 occupancy and the gauche/gauche $0 \cdot 375$. The major component forms a


[^0]normal hydrogen bond with an $\mathrm{H} \cdots \mathrm{O}$ distance of $1.867 \AA$; the minor component forms a bifurcated hydrogen bond having two interactions with $\mathrm{H} \cdots \mathrm{O}$ distances of 2.151 and $2.209 \AA$ at an angle of $81^{\circ}$.

Introduction. The X-ray crystal structure of $a-\mathrm{L}-$ sorbose (Kim \& Rosenstein, 1967) revealed disorder in the orientation of the primary alcohol group between two of the three possible 'staggered' positions for the hydroxyl group. This implies two possible hydrogenbonding arrangements of comparable energy. The purpose of this neutron diffraction study was to determine the precise hydrogen-bond geometry associated with these two arrangements. Suitable transparent crystals of good optical quality were obtained by slow evaporation from an ethanol-water solution. One $h k l$ octant and part of an $h \bar{k} l$ octant of neutron diffraction
data were collected using an octagonal crystal of volume $8.5965 \mathrm{~mm}^{3}$ at room temperature on the Brookhaven High Flux Beam Reactor single-crystal diffractometer by the procedure described by Takagi \& Jeffrey (1977a). The unit-cell parameters were determined by a least-squares procedure from 29 high $2 \theta$ reflections. The values agree with those from the X-ray determination within $2 \sigma$. The structure refinement data are given in Table 1.

## Table 1. Structure refinement data for a-L-sorbopyranose

Morphology: octahedron with faces $\{011\},\{110\}$.
$\mu$ (neutron) $=0.2574 \mathrm{~mm}^{-1}$; maximum and minimum corrections 1.615, 1.499.

Intensities: $2003 h k l$ and $h \bar{k} l$ measured with $\theta / 2 \theta$ step-scan and width $\Delta 2 \theta=2.4^{\circ}$ for $2 \theta<60^{\circ} ; 2.0+1.4 \tan \theta$ for $60<2 \theta<$ $105^{\circ}$. Agreement between absorption-corrected symmetryequivalent $F_{h k l}$ and $F_{h \bar{k} l}$ was $R_{F}=0.030$. Intensities were averaged to give 1611 symmetry-unique data of which 1437 had $F^{2}>\sigma\left(F^{2}\right)$.
The parameter refinement was on $R_{w F^{\prime}}=\left(\left\lfloor\omega F_{o}-k F_{c}{ }^{2 / w} w F_{o}^{2}\right)^{1 / 2}\right.$, with $w^{-1}=\left[\sigma_{c}^{2}\left(F_{o}^{2}\right)+\left(0.02 F_{o}^{2}\right)^{2} \mid / 4 F_{o}^{2}\right.$.
Refined extinction parameter, $g=2.4$ (3) $\times 10^{-4}$ (Coppens \& Hamilton, 1970).
Final agreement was $R_{F}=0.044, R_{w F}=0.037$ for 1437 data,

$$
R_{F}^{\prime}=0.064, R_{w F}^{w F}=0.044 \text { for all } 1611
$$

Table 2. Fractional atomic coordinates $\left(\times 10^{4}\right)$ for $\alpha$-L-sorbopyranose

The standard deviations are given in parentheses.

|  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{C}(1 A)$ | 5293 (21) | 1691 (5) | 5127 (19) |
| $\mathrm{C}(1 B)$ | 5397 (30) | 1521 (9) | 5350 (31) |
| $\mathrm{C}(2)$ | 3942 (3) | 1197 (1) | 3716 (2) |
| $\mathrm{C}(3)$ | 3363 (2) | 1665 (1) | 1770 (2) |
| C(4) | 1762 (2) | 1274 (1) | 416 (2) |
| C(5) | -63 (2) | 1047 (1) | 1763 (2) |
| C(6) | 648 (3) | 619 (1) | 3699 (3) |
| $\mathrm{O}(1 /$ ) | 6310 (17) | 1243 (9) | 6642 (16) |
| $\mathrm{O}(1 B)$ | 4722 (37) | 2185 (11) | 6087 (34) |
| $\mathrm{O}(2)$ | 4897 (3) | 556 (1) | 2976 (3) |
| $\mathrm{O}(3)$ | 5110 (3) | 1808 (1) | 526 (3) |
| $\mathrm{O}(4)$ | 1135 (4) | 1755 (1) | -1239 (3) |
| O(5) | -1376 (3) | 592 (1) | 534 (4) |
| O (6) | 2144 (3) | 1023 (1) | 4881 (3) |
| $\mathrm{H}(\mathrm{C} 1 A) 1$ | 6390 (20) | 1991 (6) | 4200 (23) |
| $\mathrm{H}(\mathrm{C} 1 A) 2$ | 4458 (47) | 2102 (14) | 6079 (46) |
| $\mathrm{H}(\mathrm{C} 1 B) 1$ | 5763 (40) | 1170 (24) | 6735 (61) |
| $\mathrm{H}(\mathrm{C} 1 B) 2$ | 6827 (26) | 1674 (12) | 4405 (31) |
| H(C3) | 2688 (6) | 2188 (2) | 2361 (6) |
| H(C4) | 2451 (6) | 773 (2) | -279 (6) |
| H(C5) | -865 (6) | 1557 (2) | 2254 (7) |
| H(C6)1 | 1279 (8) | 87 (2) | 3158 (9) |
| H(C6)2 | -614 (7) | 514 (3) | 4789 (8) |
| $\mathrm{H}(\mathrm{O} 1 A)$ | 6029 (15) | 1372 (6) | 8017 (12) |
| $\mathrm{H}(\mathrm{O} 1 B)$ | 4098 (36) | 2089 (8) | 7385 (25) |
| $\mathrm{H}(\mathrm{O} 2)$ | 5403 (6) | 260 (3) | 4143 (7) |
| H(O3) | 5545 (6) | 2317 (2) | 762 (6) |
| H(04) | 1281 (9) | 1526 (3) | -2570 (6) |
| $\mathrm{H}(\mathrm{O} 5)$ | -2737 (6) | 626 (3) | 1100 (9) |

The non-hydrogen atom coordinates and the occupancy factors for the $\mathrm{O}(1)$ disorder from the X-ray analysis were used to calculate the phases and a difference Fourier synthesis, which showed all the H atoms except those attached to $\mathrm{O}(1)$. Fourier refinement, followed by isotropic and anisotropic leastsquares refinement, with an isotropic extinction parameter, gave the final atomic parameters given in Table 2. The resolution of the disorder was unconvincing until it was realized, from a difference synthesis, that the $C(1)$ atoms were also disordered. A stereoview of the molecule is shown in Fig. 1; the molecular dimensions are given in Fig. 2.*

Discussion. The molecule has the ${ }^{2} C_{5}$-(L) conformation, which is very close to an ideal chair as shown by the puckering parameters (Cremer \& Pople, 1975); $\theta=$ $178.3, \varphi=138.7^{\circ}, Q=0.553, q_{2}=0.017, q_{3}=$ $-0.553 \AA$. The $\mathrm{C}-\mathrm{C}$ bond lengths, excluding $C(1)-C(2)$, vary by $0.020 \AA(10 \sigma)$ with a mean of

[^1]


Fig. 1. Stereoview of $\alpha$-L-sorbopyranose. The minor component of the disorder is shown by the open lines.


Fig. 2. Bond lengths ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ of $a-\mathrm{L}$-sorbopyranose. Those of the minor component of the disordered primary alcohol group are shown in the top right-hand corner. The bond length $\sigma$ s are $\mathrm{C}-\mathrm{C}, 0.002 ; \mathrm{C}-\mathrm{O}, 0.003 ; \mathrm{C}-\mathrm{H}, 0.004 ; \mathrm{O}-\mathrm{H}, 0.005 \AA$. The bond angle $\sigma$ s are $\mathrm{C}-\mathrm{C}-\mathrm{C}, 0 \cdot 1 ; \mathrm{C}-\mathrm{C}-\mathrm{O}, 0 \cdot 2 ; \mathrm{C}-\mathrm{O}-\mathrm{H}$, $\mathrm{C}-\mathrm{C}-\mathrm{H}$, and $\mathrm{O}-\mathrm{C}-\mathrm{H}, 0.3: \mathrm{H}-\mathrm{C}-\mathrm{H}, 0.4^{\circ}$. Bond angles not included in the figure have been deposited.


Fig. 3. Hydrogen bonding in $\alpha$-L-sorbopyranose. (a) The infinite chain, $(b)$ the finite chain.
$1.5258 \AA(0.01 \AA$ longer than the mean X-ray values); the $\mathrm{C}-\mathrm{O}$ bond lengths, with the exception of the hemiacetal group, vary by $0.010 \AA(3 \sigma)$ with a mean of $1.4178 \AA$. The $\mathrm{C}-\mathrm{O}$ bond lengths in the hemiacetal moiety have $\mathrm{C}(6)-\mathrm{O}(6)>\mathrm{O}(6)-\mathrm{C}(2)>\mathrm{C}(2)-\mathrm{O}(2)$, in agreement with the prediction from ab initio quantummechanical calculations of the model compound, $\mathrm{H}_{3} \mathrm{C}-$ $\mathrm{O}-\mathrm{CH}_{2}-\mathrm{OH}$, in which the optimized values were 1.444, 1.421 and $1.417 \AA$ (Jeffrey, Pople \& Radom, 1974). The C-H bond lengths vary by $0.040 \AA$ (10 $\sigma$ ) with a mean of $1 \cdot 1030 \AA$; the $\mathrm{O}-\mathrm{H}$ bond lengths vary
by $0.031 \AA(6 \sigma)$ with a mean of $0.9615 \AA$. Those of the disordered hydroxyls are foreshortened due to increased thermal motion.
The disorder of the primary alcohol group is 0.625 gauche/trans and 0.375 gauche/gauche, these being the two preferred staggered orientations which avoid the syndiaxial interaction with $\mathrm{O}(3) \mathrm{H}$.
The hydrogen bonding is shown in Fig. 3. It consists of infinite and finite chains. The infinite chains, which link the $\mathrm{O}(2) \mathrm{H}$ and $\mathrm{O}(5) \mathrm{H}$ hydroxyls in a spiral arrangement, have longer than average $\mathrm{H} \cdots \mathrm{O}$ distances; 1.882 and $1.953 \AA$ versus $1.815 \AA$ for the mean of 25 neutron diffraction observations for bonds of this type (Jeffrey \& Takagi, 1978). However, O(5)H is also involved in a weak interaction with $\mathrm{O}(3)$ at $2.582 \AA$, forming an asymmetrical bifurcated hydrogen bond (see Jeffrey \& Takagi, 1978; Newton, Jeffrey \& Takagi, 1979), similar to that observed in the neutron diffraction study of $\beta$-D-fructopyranose (Takagi \& Jeffrey, 1977b). The finite chains, which originate at $\mathrm{O}(1 A)$ or $\mathrm{O}(1 B)$ and terminate at the ring oxygens, have a short central $\mathrm{H} \cdots \mathrm{O}$ bond of $1.746 \AA$. The bond to the ring $\mathrm{O}(6)$ atom agrees well with the mean value of $1.954 \AA$ for 11 neutron and X-ray data (Jeffrey \& Takagi, 1978). When $\mathrm{O}(1 B)-\mathrm{H}$ substitutes for $\mathrm{O}(1 \mathrm{~A})-\mathrm{H}$, the normal hydrogen bond of length 1.867 $\AA$ is replaced by a bifurcated interaction with two $\mathrm{H} \cdots \mathrm{O}$ bonds of 2.151 and $2.209 \AA$ at an angle of $81^{\circ}$. This is similar to the bifurcated hydrogen bonds observed in methyl $a$-D-altropyranoside (Poppleton, Jeffrey \& Williams, 1975). It can be inferred that the bifurcated interaction is comparable in energy to the normal linear hydrogen bond. Ab initio calculations on model systems give theoretical support for that view (Newton, Jeffrey \& Takagi, 1979).

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    $\dagger$ Present address: Department of Chemistry, University of Oslo, PO Box 1033, Blindern, Oslo 3, Norway.
    $\ddagger$ Present address: American Dental Association, Health Foundation Research Unit, National Bureau of Standards, Washington, DC 20234, USA.

[^1]:    * Lists of structure factors, bond angles not included in Fig. 2, and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34149 ( 13 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

